

707.009

Foundations of Knowledge Management „Inductive Concept Learning and ILP“

How can we uncover conceptual relations
from examples / background knowledge?

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...the following resources:

- “Inductive Logic Programming: Theory and Methods”
 - Stephen Muggleton and Luc de Raedt
- “Inductive Logic Programming: Techniques and Applications”
 - Nada Lavrac and Saso Dzeroski
- Slides “Introduction to Inductive Logic Programming”
 - Nada Lavrac
- Slides “Inductive Logic Programming: Basic Approaches”
 - Chongbing Liu

Overview

Today's Agenda:

Inductive Concept Learning & ILP

- Problem Definition
- Success Criteria
- Inductive Logic Programming
- Selected ILP Techniques

Wissensorganisation – Zwei Herangehensweisen

Formale vs. inhaltliche Struktur

Viele Informationen liegen in unstrukturierten Freitexten (Inhalt ohne Struktur) vor. Aussagekräftig aber schlecht auswertbar

Zwei Herangehensweisen:

- Verwendung einer standardisierten Sprache a **priori** (stark formalisiert)
- Interpretation der heterogenen Sprache a **posteriori** (NLP, ...)

Taxonomien,
Ontologien,
Semantische
Netze

Schlüsselwort-
extraktion,
Folksonomies



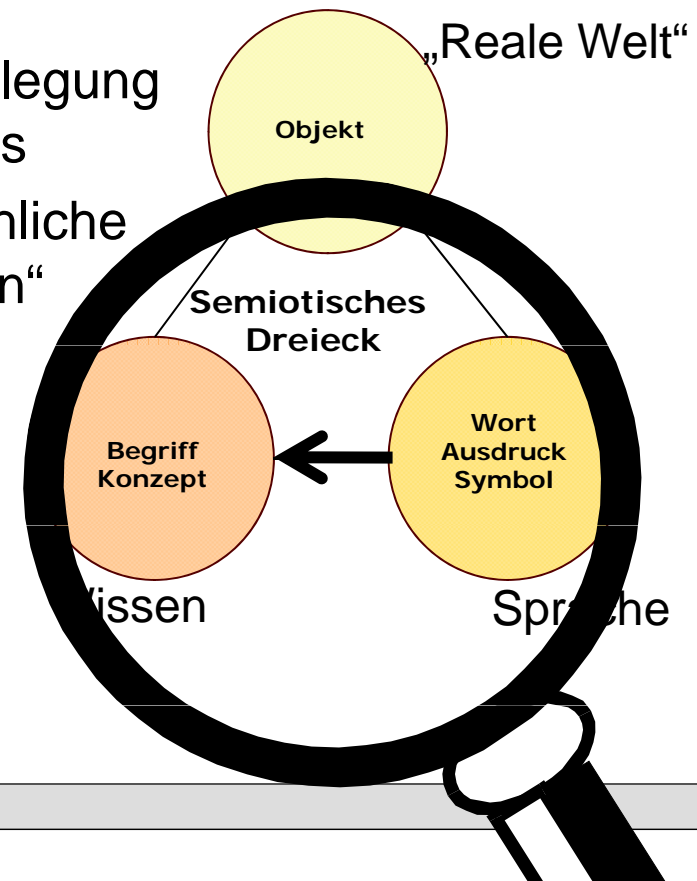
Was sind Konzeptsysteme?

Konzeptsysteme sind Systeme von unterscheidbaren *Konzepten*, die mittels *Relationen* in Beziehung zueinander gesetzt werden und in einer natürlicheren *Sprache* formuliert werden können



Zielsetzung: Entwicklung und Festlegung eines gemeinsamen Verständnisses

Repräsentationssysteme: menschliche Sprache, Logik, „Computersprachen“



Inductive Concept Learning

$daughter(X, Y) \leftarrow ?$

How would you define the $daughter(X, Y)$ relationship based on 1) Background K and 2) Training examples?

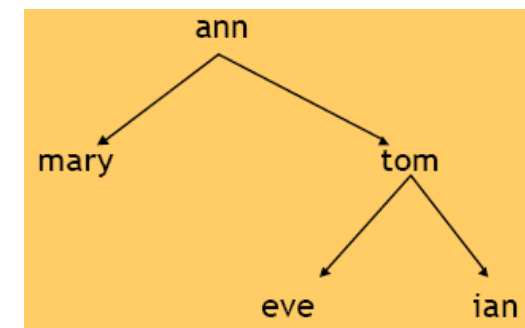
<i>Training examples</i>	
$daughter(mary, ann).$	\oplus
$daughter(eve, tom).$	\oplus
$daughter(tom, ann).$	\ominus
$daughter(eve, ann).$	\ominus

<i>Background knowledge</i>	
$parent(ann, mary).$	$female(ann).$
$parent(ann, tom).$	$female(mary).$
$parent(tom, eve).$	$female(eve).$
$parent(tom, ian).$	

$c = daughter(X, Y) \leftarrow female(X), parent(Y, X)$

Inductive Concept Learning

- $E^+ = \{\text{daughter}(\text{mary}, \text{ann}), \text{daughter}(\text{eve}, \text{tom})\}$
 $E^- = \{\text{daughter}(\text{tom}, \text{ann}), \text{daughter}(\text{eve}, \text{ann})\}$
- $B = \{\text{mother}(\text{ann}, \text{mary}), \text{mother}(\text{ann}, \text{tom}),$
 $\text{father}(\text{tom}, \text{eve}), \text{father}(\text{tom}, \text{ian}), \text{female}(\text{ann}),$
 $\text{female}(\text{mary}), \text{female}(\text{eve}), \text{male}(\text{ian}), \text{male}(\text{tom}),$
 $\text{parent}(X, Y) \leftarrow \text{mother}(X, Y),$
 $\text{parent}(X, Y) \leftarrow \text{father}(X, Y)\}$



The Problem of Inductive Concept Learning

U is a universal set of objects

C is a concept: a subset of objects in U $C \subseteq U$

To learn a concept C means to learn to recognize objects in C, to be able to tell whether

$x \in C$ for each $x \in U$

Example:

U may be the set of all patients in a register, and $C \subseteq U$

The set of all patients having a particular disease

Describing objects and concepts

Objects are described in *object description languages*

Concepts are described in *concept description languages*

Describing Objects:

In attribute-value object description languages, objects are described as attribute-value pairs.

e.g. `card(diamonds, 7)`

card is a predicate, values are the constants diamonds and 7

Describing objects and concepts

Describing Concepts:

- Extensionally:
 - Listing the descriptions of all of its instances
 - Example: *Pair* in poker can be extensionally described by the set of all pairs of cards which have the same rank
- Intensionally:
 - In a separate concept description language which allows for more compact and concise concept descriptions, e.g. in the form of rules

$$\begin{array}{l}
 \textit{pair} \text{ if } [Rank_1 = 7] \wedge [Rank_2 = 7] \vee \\
 \quad [Rank_1 = 8] \wedge [Rank_2 = 8] \vee \\
 \quad \dots \\
 \quad [Rank_1 = a] \wedge [Rank_2 = a]
 \end{array}
 \qquad
 \textit{pair} \text{ if } Rank_1 = Rank_2$$

- Horn clause: $\textit{pair}(Suit_1, Rank_1, Suit_2, Rank_2) \leftarrow Rank_1 = Rank_2$

What are the implications of describing concepts extensionally / intensionally?

Inductive Concept Learning

Is a procedure for determining whether a given object belongs to a given concept i.e. whether the description of the object satisfies the description of the concept.

Definitions:

- A **Fact** denotes an object description
- A **Hypothesis** denotes an intensional concept description
- An **example** e for learning a concept C is a labeled *fact*
- A label could be either \oplus (pos. Examples) or \ominus (neg. examples)
- ε^+ denotes the set of positive examples
- ε^- denotes the set of negative examples

Inductive Concept Learning

Inductive concept learning Given a set \mathcal{E} of positive and negative examples of a concept \mathcal{C} , find a hypothesis \mathcal{H} , expressed in a given concept description language \mathcal{L} , such that:

- every positive example $e \in \mathcal{E}^+$ is covered by \mathcal{H} ,
- no negative example $e \in \mathcal{E}^-$ is covered by \mathcal{H} .

To test the coverage, the function

covers(\mathcal{H}, e)

Returns the value true if e is covered by \mathcal{H} , and false otherwise.

Example

Is

$pair(card(diamonds, 7), card(hearts, 7))$

covered by

$pair(card(Suit_1, Rank_1), card(Suit_2, Rank_2)) \leftarrow Rank_1 = Rank_2$

?

Completeness and consistency of a hypothesis

A hypothesis H is **complete** with respect to the examples E if H covers all the positive examples.

$$\text{if } \text{covers}(\mathcal{H}, \mathcal{E}^+) = \mathcal{E}^+$$

A hypothesis H is **consistent** with respect to examples E if it covers none of the negative examples.

$$\text{if } \text{covers}(\mathcal{H}, \mathcal{E}^-) = \emptyset$$

Completeness and consistency of a hypothesis

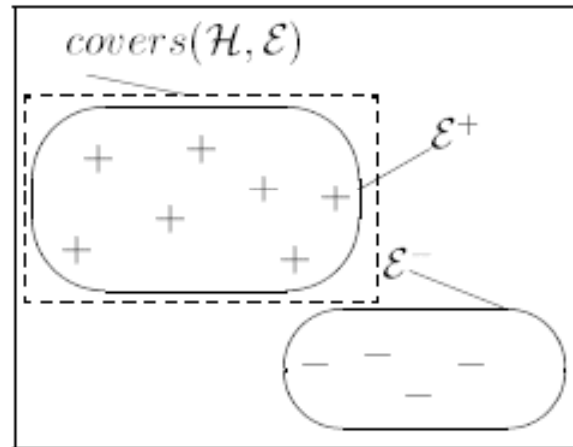
Complete:

if $covers(\mathcal{H}, \mathcal{E}^+) = \mathcal{E}^+$

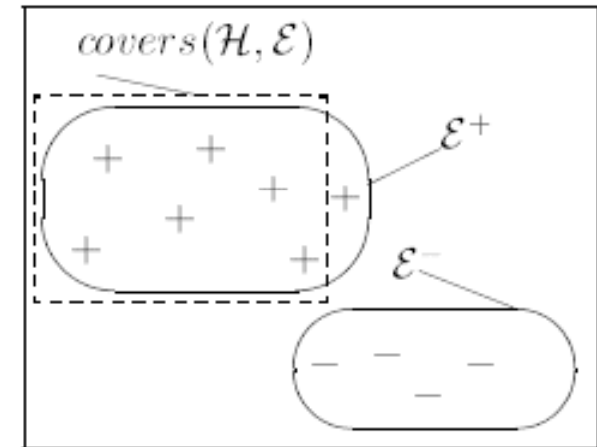
Consistent:

if $covers(\mathcal{H}, \mathcal{E}^-) = \emptyset$

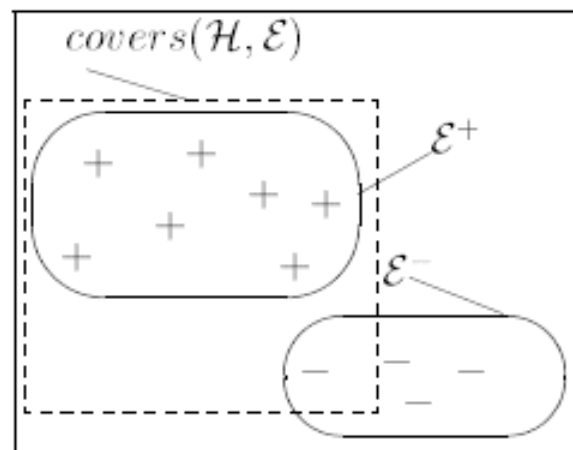
\mathcal{H} : complete, consistent



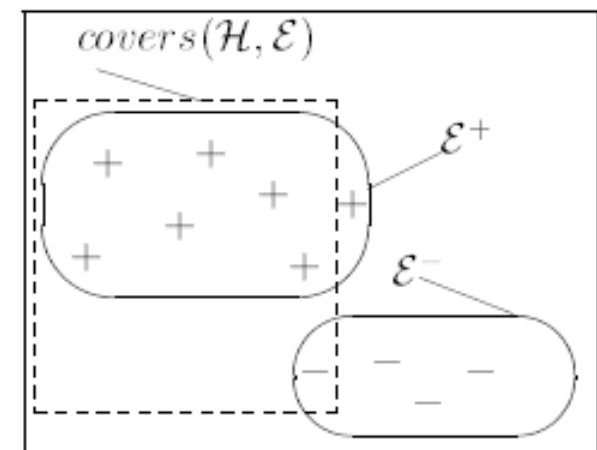
\mathcal{H} : incomplete, consistent



\mathcal{H} : complete, inconsistent



\mathcal{H} : incomplete, inconsistent



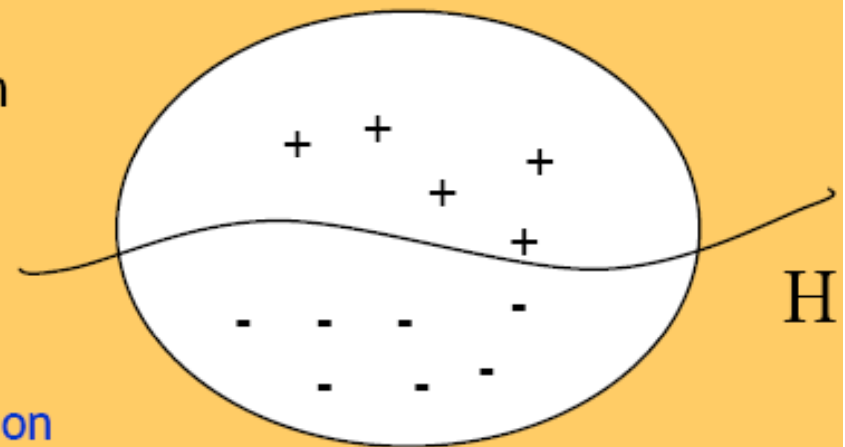
Other criteria for success

- Classification accuracy of H:
The percentage of objects correctly classified by the hypothesis
- Transparency of H:
the extent to which a hypothesis is understandable to humans

Predictive vs. Descriptive Induction

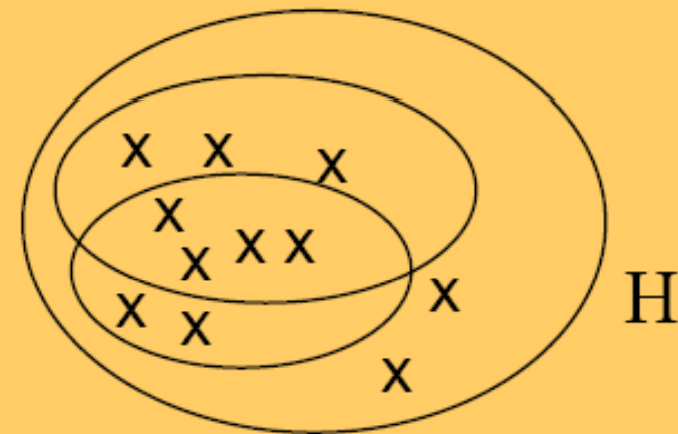
Predictive induction: Inducing classifiers, aimed at solving classification/prediction tasks

- Classification rule learning, Decision tree learning, ...
- Bayesian classifier, ANN, SVM, ..
- [Data analysis through hypothesis generation and testing](#)



Descriptive induction: Discovering regularities, uncovering patterns, aimed at solving KDD tasks

- Symbolic clustering, Association rule learning, Subgroup discovery, ...
- [Exploratory data analysis](#)



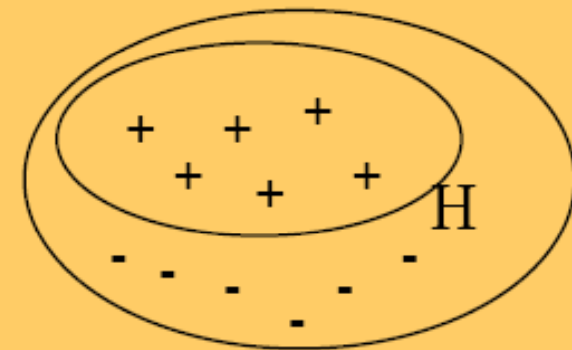
Predictive ILP

- **Given:**

- A set of observations
 - positive examples E^+
 - negative examples E^-
- background knowledge B
- hypothesis language L_H
- **covers** relation

- **Find:**

A hypothesis $H \in L_H$, such that (given B) H covers all positive and no negative examples



- In logic, **find** H such that

- $\forall e \in E^+ : B \wedge H \models e$ (H is complete)
- $\forall e \in E^- : B \wedge H \not\models e$ (H is consistent)

- In ILP, E are ground facts, B and H are (sets of) definite clauses

Predictive ILP

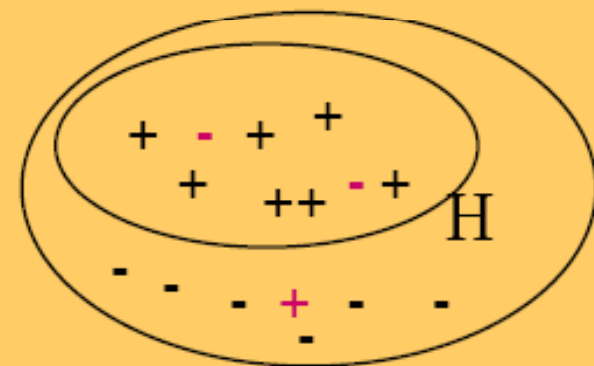
- **Given:**

- A set of observations
 - positive examples E^+
 - negative examples E^-
- background knowledge B
- hypothesis language L_H
- covers relation
- **quality criterion**

- **Find:**

A hypothesis $H \in L_H$, such that (given B) H is optimal w.r.t. some quality criterion, e.g., max. predictive accuracy $A(H)$

(**instead of** finding a hypothesis $H \in L_H$, such that (given B) H covers **all** positive and **no** negative examples)



Descriptive ILP

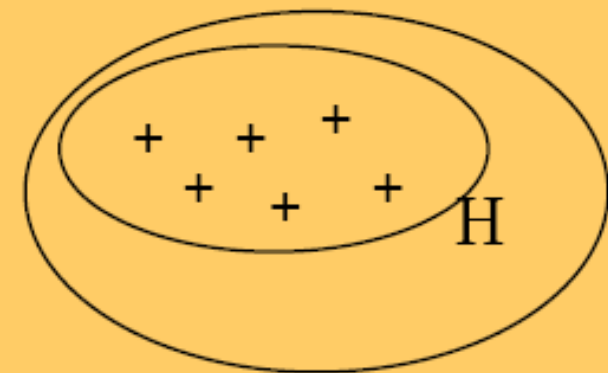
- **Given:**

- A set of observations
(positive examples E^+)
- background knowledge B
- hypothesis language L_H
- covers relation

- **Find:**

Maximally specific hypothesis $H \in L_H$, such that (given B) H covers all positive examples

- In logic, **find** H such that $\forall c \in H, c$ is true in some preferred model of $B \cup E$ (e.g., least Herbrand model $M(B \cup E)$)
- In ILP, E are ground facts, B are (sets of) general clauses



An Example ILP Problem

- The task is to define the target relation *daughter* (X,Y), which states that person X is a daughter of person Y, in terms of the **background knowledge** relations **female** and **parent**.

Answering: When is X the daughter of Y?

The Target Relation:

$$daughter(X, Y) \leftarrow female(X), parent(Y, X)$$

Training Examples:

<i>Training examples</i>		<i>Background knowledge</i>	
<i>daughter(mary, ann).</i>	⊕	<i>parent(ann, mary).</i>	<i>female(ann).</i>
<i>daughter(eve, tom).</i>	⊕	<i>parent(ann, tom).</i>	<i>female(mary).</i>
<i>daughter(tom, ann).</i>	⊖	<i>parent(tom, eve).</i>	<i>female(eve).</i>
<i>daughter(eve, ann).</i>	⊖	<i>parent(tom, ian).</i>	

Potential Target Predicate Relations:

$$daughter(X, Y) \leftarrow female(X), mother(Y, X)$$

$$daughter(X, Y) \leftarrow female(X), father(Y, X)$$

Different ILP Learners

- Single concept learners and multiple concepts learners
- Batch learners and incremental learners
- Non-Interactive learners and interactive learners

Empirical ILP Learners:

non-interactive single concept batch learners

An Simple Example

- Training Examples

$\mathcal{E}^+ = \{ \text{daughter}(\text{mary}, \text{ann}).$
 $\text{daughter}(\text{eve}, \text{tom}). \}$

$\mathcal{E}^- = \{ \text{daughter}(\text{tom}, \text{ann}).$
 $\text{daughter}(\text{eve}, \text{ann}). \}$

- Concept learned:

$\text{daughter}(X, Y) \leftarrow \text{female}(X), \text{parent}(Y, X)$

- Background Knowledge

$\text{parent}(\text{ann}, \text{mary}).$

$\text{parent}(\text{ann}, \text{tom}).$

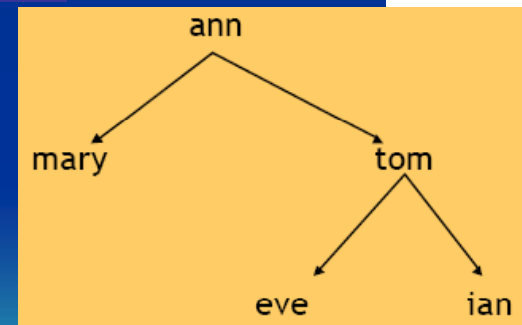
$\text{parent}(\text{tom}, \text{eve}).$

$\text{parent}(\text{tom}, \text{ian}).$

$\text{female}(\text{ann}).$

$\text{female}(\text{mary}).$

$\text{female}(\text{eve}).$



Sample problem

Knowledge discovery

- $E^+ = \{daughter(mary,ann), daughter(eve,tom)\}$
 $E^- = \{daughter(tom,ann), daughter(eve,ann)\}$
- $B = \{mother(ann,mary), mother(ann,tom), father(tom,eve),$
 $father(tom,ian), female(ann), female(mary), female(eve),$
 $male(ian), male(tom), parent(X,Y) \leftarrow mother(X,Y), parent(X,Y) \leftarrow father(X,Y)\}$

- **Predictive ILP - Induce a definite clause**

$daughter(X,Y) \leftarrow female(X), parent(Y,X).$

or a set of definite clauses

$daughter(X,Y) \leftarrow female(X), mother(Y,X).$

$daughter(X,Y) \leftarrow female(X), father(Y,X).$

- **Descriptive ILP - Induce a set of (general) clauses**

$\leftarrow daughter(X,Y), mother(X,Y).$

$female(X) \leftarrow daughter(X,Y).$

$mother(X,Y); father(X,Y) \leftarrow parent(X,Y).$

Generality

Generality: Let C and D be two clauses.

C is more general than D iff

$C \models D$, i.e., iff $\text{cov}(D) \subseteq \text{cov}(C)$

Note: Logical entailment (even between Horn clauses) is undecidable.

Subsumption

Substitution: $\theta = \{X_1/t_1, \dots, X_n/t_n\}$ is an assignment of terms t_i to variables X_i

Subsumption: Let C and D be two clauses.
 C subsumes D iff there is a θ , such that
 $C\theta \subseteq D$

Example: $p(a,b) \leftarrow r(b,a)$
 is subsumed by $(\theta = \{X/a, Y/b\})$

$p(X,Y) \leftarrow r(Y,X)$

subsumes

$p(X,Y) \leftarrow r(Y,X), q(X)$

Note: Subsumption is decidable (but NP complete)

Note: if C subsumes D , then $C \models D$. The reverse is not always true !

Substitution, Subsumption

Example 2.1 (Substitution, subsumption)

Let c be the clause:

$$c = \text{daughter}(X, Y) \leftarrow \text{parent}(Y, X)$$

A substitution $\theta = \{X/\text{mary}, Y/\text{ann}\}$ applied to clause c is obtained by applying θ to each of its literals:

$$c\theta = \text{daughter}(\text{mary}, \text{ann}) \leftarrow \text{parent}(\text{ann}, \text{mary})$$

Clause c θ -subsumes the clause

$$c' = \text{daughter}(X, Y) \leftarrow \text{female}(X), \text{parent}(Y, X)$$

under the empty substitution $\theta = \emptyset$, since the set

$$\{\text{daughter}(X, Y), \overline{\text{parent}(Y, X)}\}$$

is a proper subset of $\{\text{daughter}(X, Y), \overline{\text{female}(X)}, \overline{\text{parent}(Y, X)}\}$.

X is EITHER the daughter of Y OR Y is not the parent of X

$$\text{daughter}(X, Y) \leftarrow \text{parent}(Y, X) \text{ equiv. to } \{\text{daughter}(X, Y), \overline{\text{parent}(Y, X)}\}$$

Substitution, Subsumption

Let c be the clause:

$$c = \text{daughter}(X, Y) \leftarrow \text{parent}(Y, X)$$

Clause c θ -subsumes the clause

$$c' = \text{daughter}(X, X) \leftarrow \text{female}(X), \text{parent}(X, X)$$

under the substitution $\theta = \{Y/X\}$.

Clause c θ -subsumes the clause

$$\begin{aligned} \text{daughter}(\text{mary}, \text{ann}) \leftarrow & \text{female}(\text{mary}), \\ & \text{parent}(\text{ann}, \text{mary}), \\ & \text{parent}(\text{ann}, \text{tom}) \end{aligned}$$

under the substitution $\theta = \{X/\text{mary}, Y/\text{ann}\}$.

Substitution, Subsumption

Two important properties:

If $c \oplus$ -subsumes c' then c logically entails c' , $c \models c'$

The relation \leq introduces a lattice on the set of reduced clauses

ILP as a search of program clauses

An ILP learner can be described by

- the **structure of the space of clauses**
- its **search strategy**
- uninformed search (depth-first, breadth-first, iterative deepening)
- heuristic search (best-first, hill-climbing, beam search)
 - its **heuristics**
 - for directing search
 - for stopping search (quality criterion)

Learning

Two strategies for learning

- Top-down search of refinement graphs
- Bottom-up search
 - building least general generalizations
 - inverting resolution (CIGOL)
 - inverting entailment (PROGOL)

Refinement operator

$C \rightarrow \text{ref}(C)$

Minimal (most general) specialization:

D is subsumed by C, but there is no more general D' which is also subsumed by C.

- Apply a substitution θ to the clause
- Add a literal to the clause

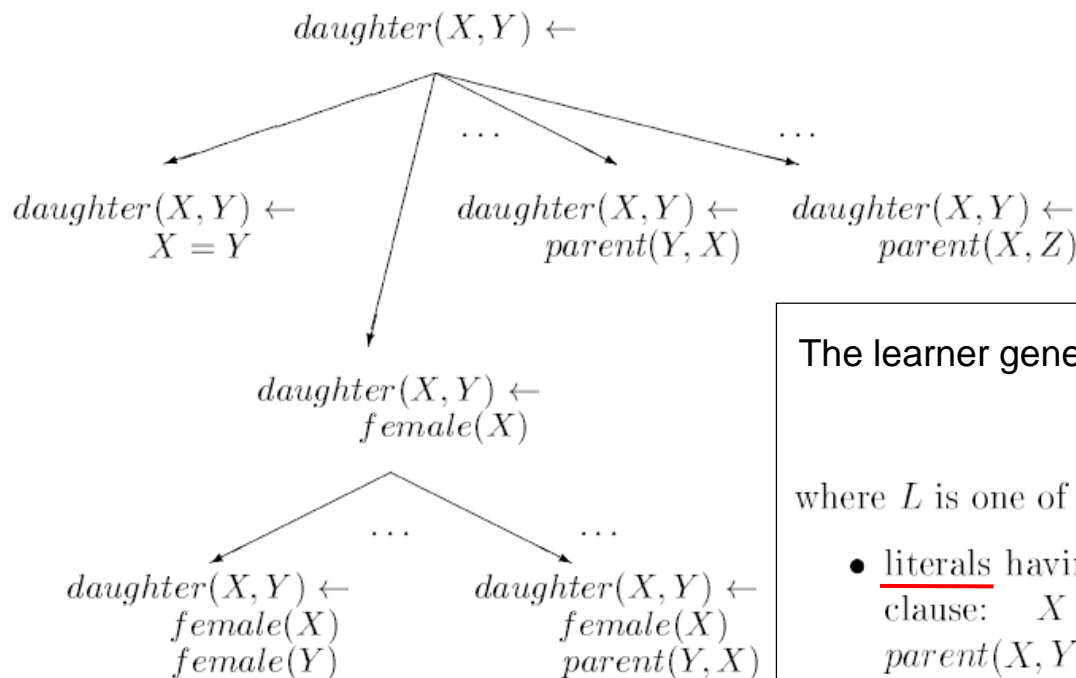
Refinement operator defines the specialization graph.

The hypothesis language has to be specified: predicates, functors, constants, (types of arguments).

Size of the search space increases with the number of existential variables in the body.

Top-Down Search of Refinement Graphs

Top down learners start from the most general clauses and repeatedly refine (specialize) them until they no longer cover negative examples.



The learner generates the set of refinements / clauses:

$$\rho(c) = \{daughter(X,Y) \leftarrow \underline{L}\}$$

where L is one of following literals:¹

- literals having as arguments the variables from the head of the clause: $X = Y$, $female(X)$, $female(Y)$, $parent(X,X)$, $parent(X,Y)$, $parent(Y,X)$, and $parent(Y,Y)$, and
- literals that introduce a new distinct variable Z ($Z \neq X$ and $Z \neq Y$) in the clause body: $parent(X,Z)$, $parent(Z,X)$, $parent(Y,Z)$, and $parent(Z,Y)$,

Structuring the Hypothesis Space

$daughter(X, Y) \leftarrow ?$

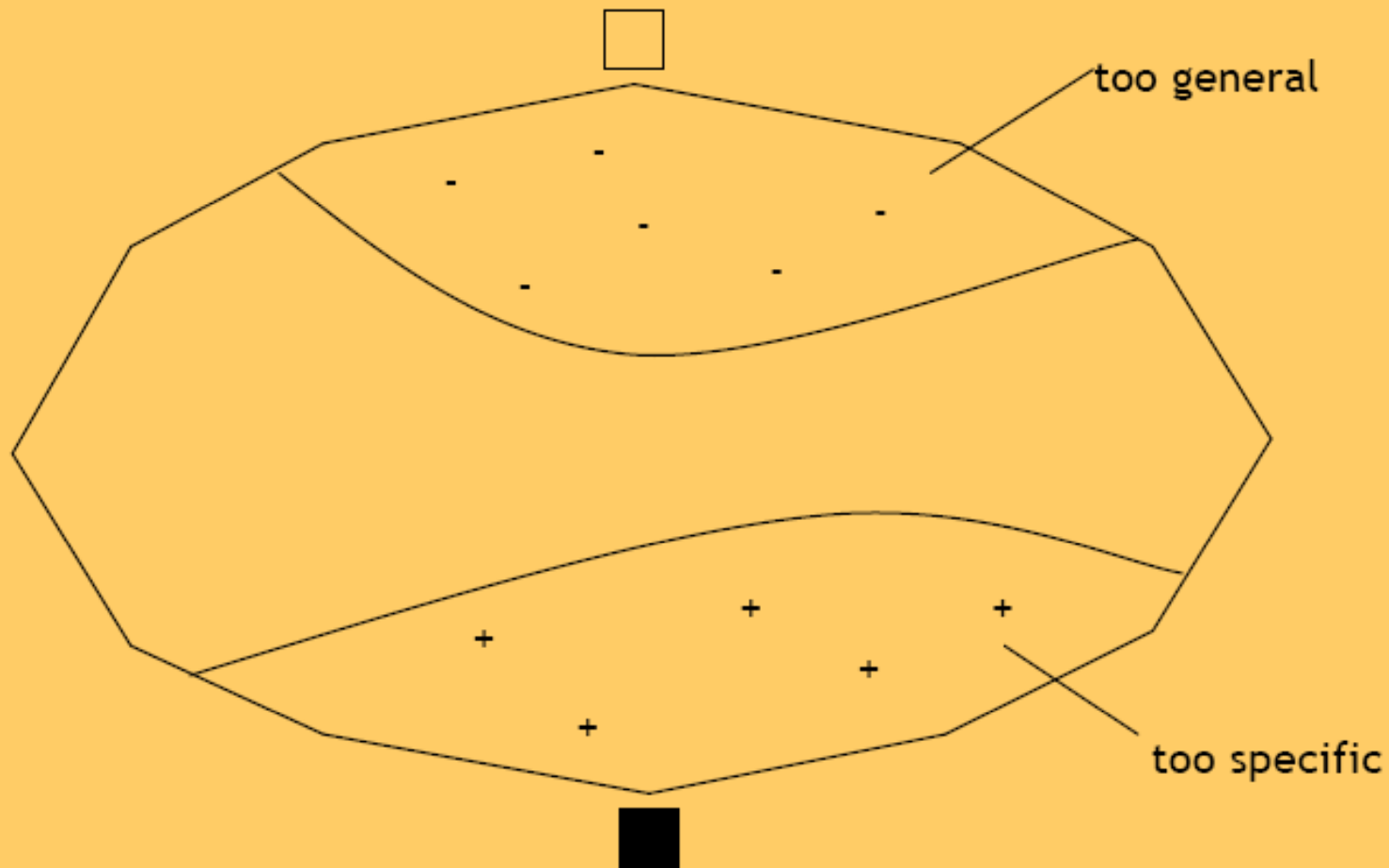
In ILP, the search space is determined by the language of logic programs \mathcal{L} consisting of program clauses of the form $T \leftarrow Q$, where T is an atom $p(X_1, \dots, X_n)$ and Q is a conjunction of literals L_1, \dots, L_m . The vocabulary of predicate symbols q_i in the literals L_i of the body of a clause is determined by the predicates from the background knowledge \mathcal{B} . If \mathcal{L} allows for recursive predicate definitions, the predicate symbol in L_i can also be the predicate symbol p itself.

ILP as search of program clauses

- **Structure of the hypothesis space**
based on the generality relation
 - G is more general than S if and only if $\text{covers}(S) \subset \text{covers}(G)$
- **Pruning the search space**
 - If H does not cover an example e then no specialization of e will cover e
→ used with positive examples for pruning
 - If H covers an example e then all generalizations of e will also cover e
→ used with negative examples for pruning
- **Version space**
The above properties determine the space of possible solutions

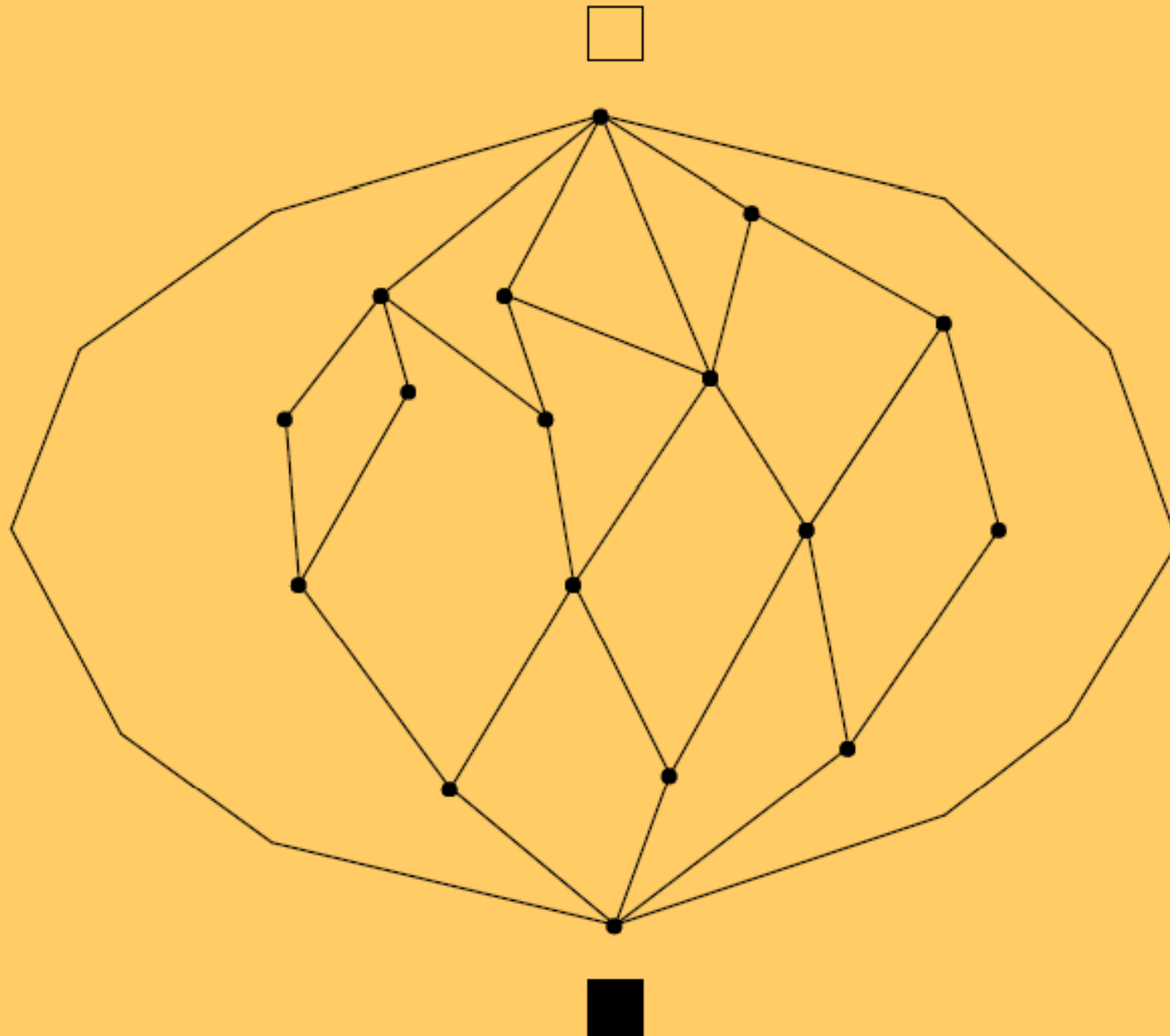
Hypothesis space

The Version Space model



How to structure the hypothesis space?
How to move from one hypothesis to another?

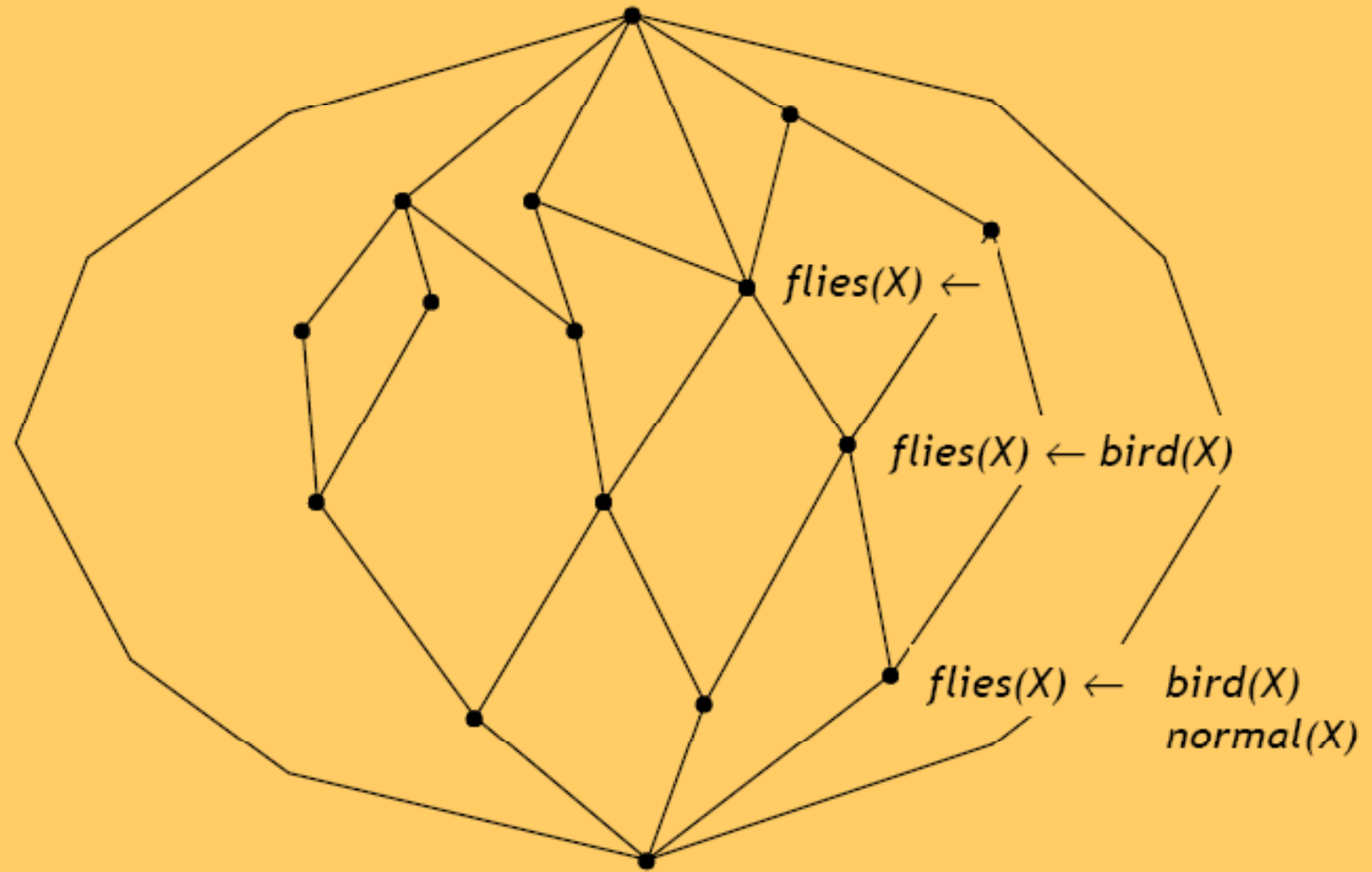
More general
(induction)



More
specific

More general
(induction)

□ = false



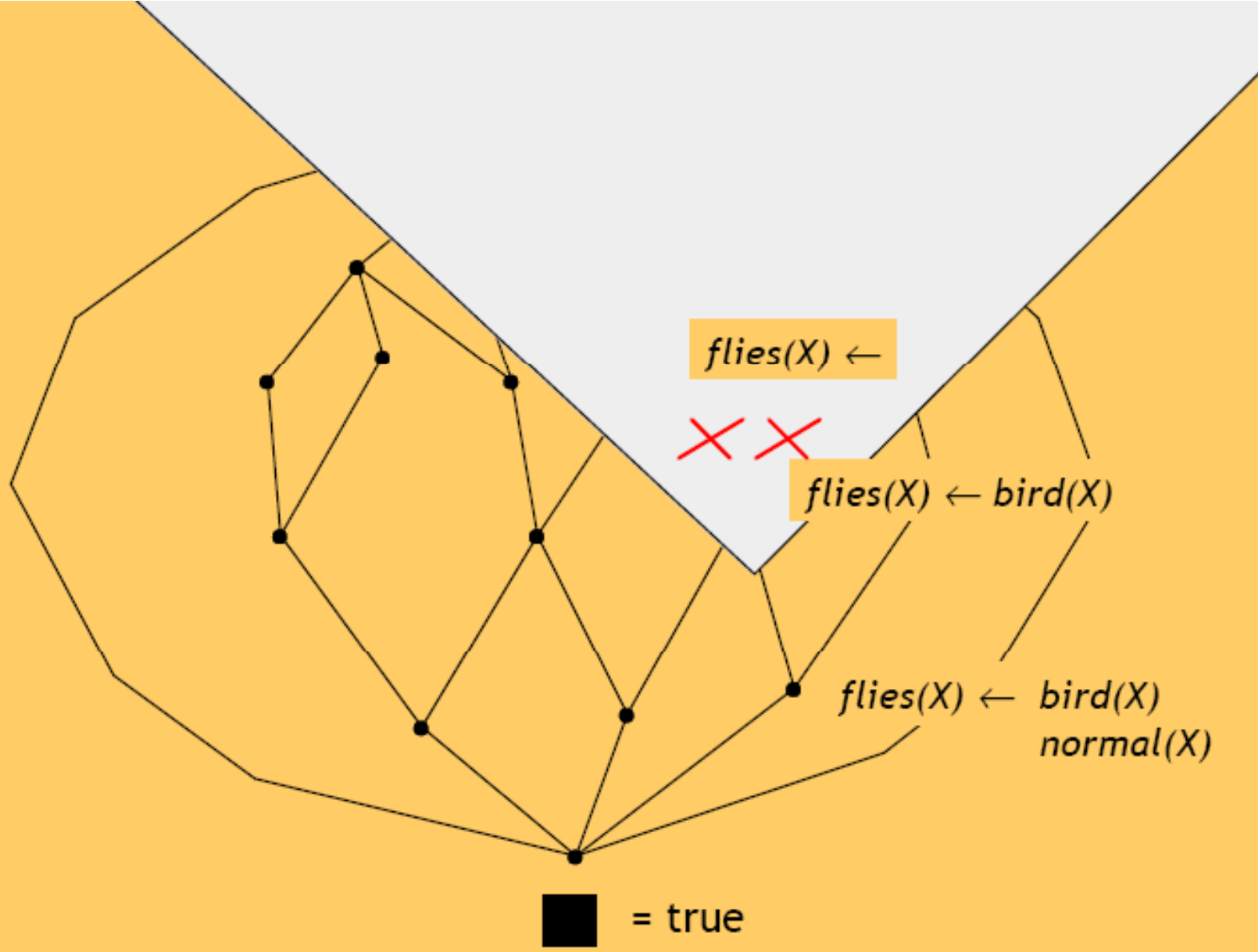
■ = true

More specific

More general
(induction)



More specific



■ = true

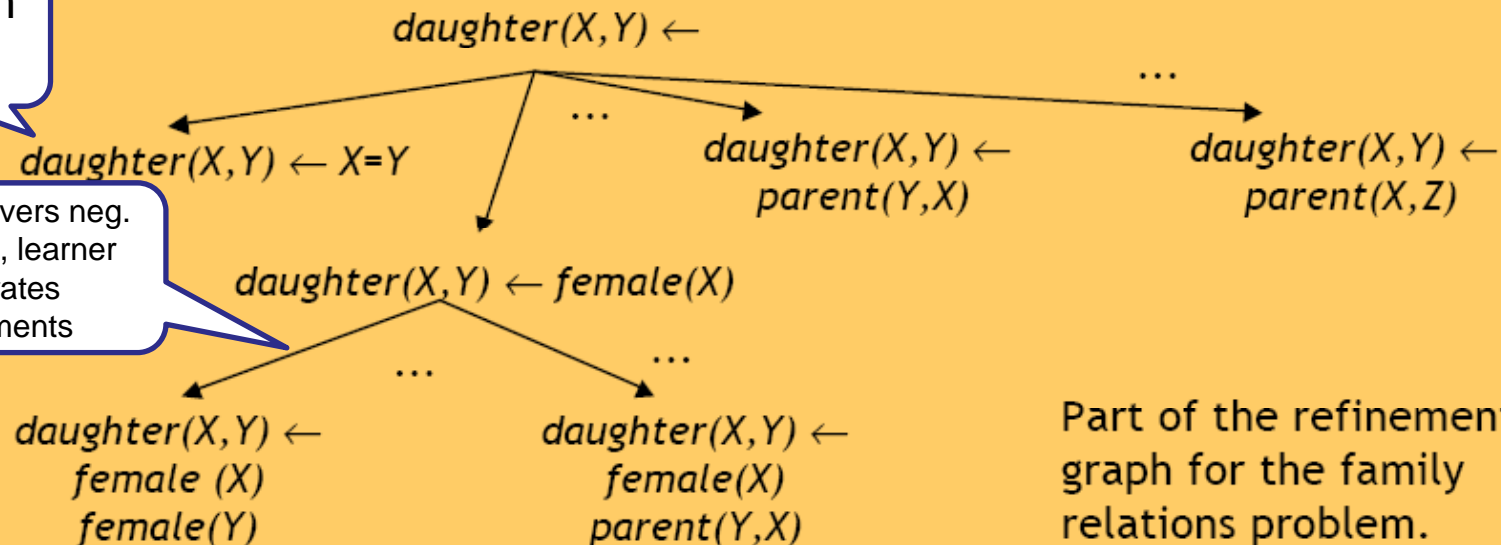
⊖ $flies(oliver) \leftarrow bird(oliver)$

Generality ordering of clauses

Training examples		Background knowledge	
daughter(mary,ann).	⊕	parent(ann,mary).	female(ann.).
daughter(eve,tom).	⊕	parent(ann,tom).	female(mary).
daughter(tom,ann).	⊖	parent(tom,eve).	female(eve).
daughter(eve,ann).	⊖	parent(tom,ian).	

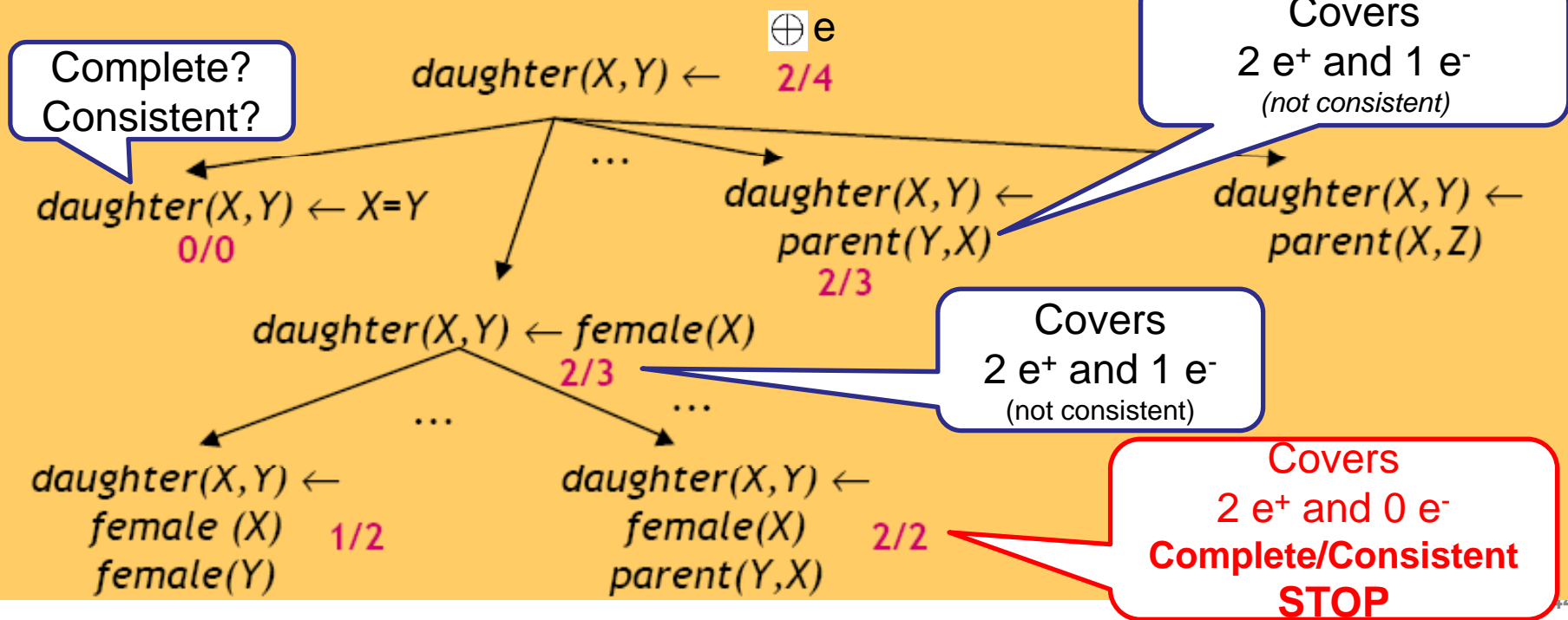
Breadth first

When c covers neg. examples, learner generates refinements



Greedy search of the best clause

Training examples		Background knowledge	
daughter(mary,ann).	⊕	parent(ann,mary).	female(ann.).
daughter(eve,tom).	⊕	parent(ann,tom).	female(mary).
daughter(tom,ann).	⊖	parent(tom,eve).	female(eve).
daughter(eve,ann).	⊖	parent(tom,ian).	



Demo

HANNE

<http://139.18.2.57:8080/hanne/org.nlp2rdf.navigator.Application/Application.html>

Conclusions

Inductive Concept Learning:

An inductive logic approach to concept learning

Comparison to Formal Concept Analysis

Requires more structured knowledge (cf. RDF,
Semantic Web!)

Any questions?

See you next week!